

12/4/17

"Our greatest weakness lies in giving up. The most certain way to succeed is always to try just one more time." -Thomas Edison

HW: Worksheet "Solving Rational Inequalities" #3, 5, 7, 9\*

AIM: How do we solve Rational Inequalities?

Warm Up:

1. Solve by completing the square:  $3x^2 + 20x + 36 = 4$

$$\begin{aligned}
 \text{Int: } \frac{20}{3} & \qquad \frac{3x^2 + 20x}{3} = \frac{-32}{3} \\
 \text{Half it: } \frac{20}{3} \div 2 = \left(\frac{10}{3}\right) & \qquad x^2 + \frac{20}{3}x + \frac{100}{9} = -\frac{32}{3} + \frac{100}{9} \\
 \text{Square } \left(\frac{10}{3}\right)^2 = \frac{100}{9} & \qquad \pm \sqrt{\left(x + \frac{10}{3}\right)^2} = \pm \sqrt{\frac{4}{9}} \\
 x = -\frac{10}{3} \pm \frac{2}{3} & \qquad x + \frac{10}{3} = \pm \frac{2}{3} \\
 -\frac{10}{3} + \frac{2}{3} = \left(-\frac{8}{3}\right) & \qquad -\frac{10}{3} = -\frac{10}{3} \\
 -\frac{10}{3} - \frac{2}{3} = -\frac{12}{3} = \left(-4\right) & 
 \end{aligned}$$

2. Solve and express your answer in interval notation:  $x^2 - 4x \leq 32$

$$\begin{aligned}
 x^2 - 4x - 32 & \leq 0 \quad \text{GOLF} \qquad \frac{-32 - 32}{x^2 - 4x - 32} \leq 0 \\
 (x - 8)(x + 4) & \\
 8 \quad -4 & \qquad -4 \quad 8 \\
 \text{Int: } [-4, 8] & 
 \end{aligned}$$

## Rational/Quadratic

### 😊 Guidelines for solving nonlinear inequalities: 😊

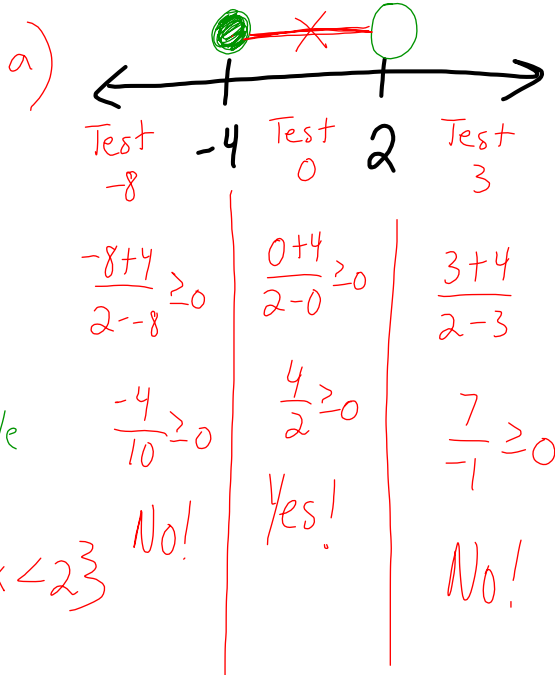
- Move all terms to one side of the inequality. (If dealing with rational expressions, get a common denominator.)
- Factor completely.
- Set each factor equal to zero. These numbers will divide your number line. (Denominator critical values ALWAYS get an open circle)
- Make a sign chart by dividing the number line into intervals found in step 3.
- Use a test value to determine the sign in each interval.
- Determine the solution of the inequality by examining the sign values.

For each inequality below, express its solution set 3 ways:

- As a number line.
- Using set-builder notation.
- Using interval notation.

1)  $\frac{x+4}{2-x} \geq 0$

$x+4=0$   
 $x=-4$   
 closed circle  
 $2-x=0$   
 $+x+x$   
 $2=x$   
 open circle

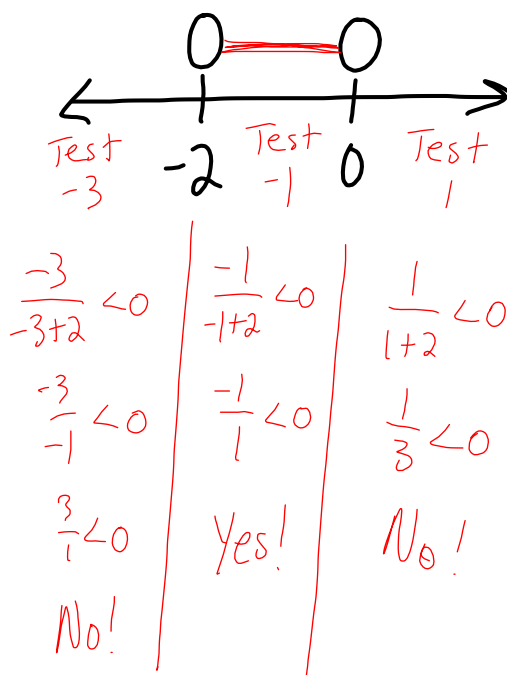


b) SB:  $\{x | -4 \leq x < 2\}$

c) Int:  $[-4, 2)$

2)  $\frac{x}{x+2} < 0$

$x=0$   
 open circles  
 $x+2=0$   
 $x=-2$   
 open circles



SB:  $\{x | -2 < x < 0\}$

Int:  $(-2, 0)$

$$3) \frac{6}{x-3} > 0$$

$$6) \frac{(6-x)(3+x)}{x+1} \leq 0$$

